

PHYS 2211K, preparation for Test 1, relations to know how to use properly

Rectilinear equations of motion:

$$\vec{r} = \vec{r}(t) = x(t)\hat{i} + y(t)\hat{j} + z(t)\hat{k} \quad (\text{the position is a function of time})$$

$$\vec{v}(t) = \frac{d\vec{r}}{dt} \quad (\text{velocity is the rate of change of position})$$

$$\vec{a}(t) = \frac{d\vec{v}}{dt} \quad (\text{acceleration is the rate of change of velocity})$$

etc.

For constant acceleration, these lead to :

$$x(t) = x_0 + v_{x0}t + \frac{1}{2}a_x t^2$$

$$y(t) = y_0 + v_{y0}t + \frac{1}{2}a_y t^2$$

$$z(t) = z_0 + v_{z0}t + \frac{1}{2}a_z t^2$$

$$v_f^2 = v_0^2 + 2ad$$

Corresponding rotational equations of motion:

$$\theta = \theta(t) \quad (\text{the angular position is a function of time})$$

$$\omega(t) = \frac{d\theta}{dt} \quad (\text{angular velocity is the rate of change of angular position})$$

$$\alpha(t) = \frac{d\omega}{dt} \quad (\text{angular acceleration is the rate of change of angular velocity})$$

For constant angular acceleration, these lead to :

$$\theta(t) = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\omega_f^2 = \omega_0^2 + 2\alpha\theta$$

For uniform circular motion:

$$a = \frac{v^2}{r}, \text{ towards the center of the circle (centripetal)}$$