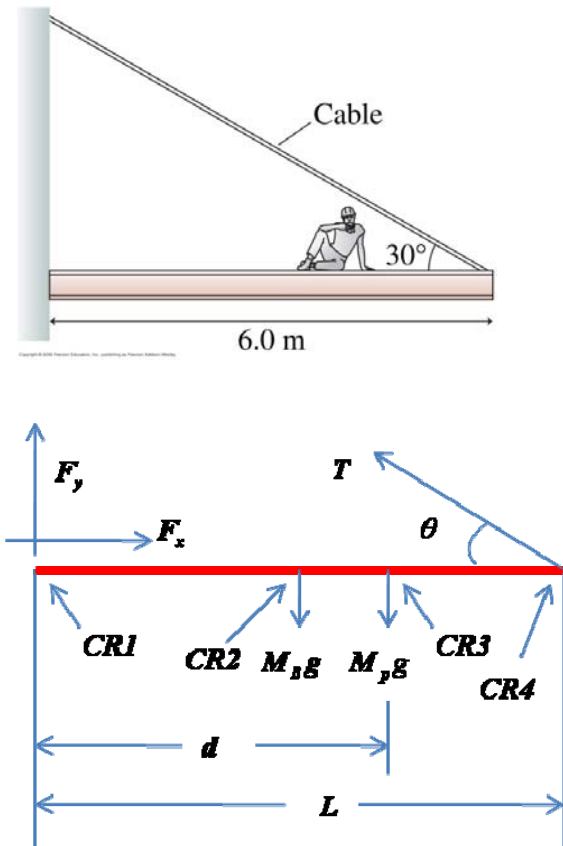


Physics 2211K, 11/2/ 2010
Quiz # 9 Solutions

In the system below, the uniform beam has mass M_B & length L , the person has mass M_p , and the cable's breaking strength is T_{max} . (Use $g = 10 \text{ m/s}^2$.)

- What is the maximum **distance from the wall** (d) the person can be without the tension in the cable exceeding the breaking point?
- Calculate the x- and y- components of the force the wall exerts on the beam.



Analysis:

Forces

$$x : 0 = F_x - T \cos \theta \Rightarrow F_x = T \cos \theta$$

$$y : 0 = F_y + T \sin \theta - M_B g - M_p g \Rightarrow F_y = (M_B + M_p) g - T \sin \theta$$

Torques

$$\tau_{cw} = \tau_{ccw}$$

$$CR1 : \left(\frac{L}{2} \right) M_B g + (d) M_p g = (L) T \sin \theta$$

$$\text{Thus, } d_{max} = \frac{(L) T_{max} \sin \theta - \left(\frac{L}{2} \right) M_B g}{M_p g}$$

Other possible CR's :

$$CR2 : \left(\frac{L}{2} \right) F_y + \left(d - \frac{L}{2} \right) M_p g = \left(\frac{L}{2} \right) T \sin \theta$$

$$CR3 : (d) F_y = \left(d - \frac{L}{2} \right) M_B g + (L - d) T \sin \theta$$

$$CR4 : (L) F_y = \left(\frac{L}{2} \right) M_B g + (L - d) T \sin \theta$$

Note : The relations for all CR's reduce to that for CR1 after substituting the expression for F_y . Thus, the choice of CR is unimportant if the torques are expressed correctly.

Ver. 1 $M_B = 1800 \text{ kg}$, $M_p = 75 \text{ kg}$, and $T_{max} = 17,500 \text{ N}$. (Use $g = 10 \text{ m/s}^2$.)

$d_{max} = -2\text{m}$ (beam will fall regardless!!) @ T_{max} , $F_x = 15155 \text{ N}$; $F_y = 10000 \text{ N}$

Ver. 2 $M_B = 1500 \text{ kg}$, $M_p = 100 \text{ kg}$, and $T_{max} = 15,000 \text{ N}$. (Use $g = 10 \text{ m/s}^2$.)

$d_{max} = 0\text{m}$ (Can't be on the beam!!) @ T_{max} , $F_x = 12990 \text{ N}$; $F_y = 8500 \text{ N}$

Ver. 3 $M_B = 2000 \text{ kg}$, $M_p = 100 \text{ kg}$, and $T_{max} = 18,000 \text{ N}$. (Use $g = 10 \text{ m/s}^2$.)

$d_{max} = -6\text{m}$ (beam will fall regardless!!) @ T_{max} , $F_x = 15588 \text{ N}$; $F_y = 12000 \text{ N}$