

Chapter 5. Force and Motion

In this chapter we study causes of motion: Why does the windsurfer blast across the water in the way he does? The combined forces of the wind, water, and gravity accelerate him according to the principles of dynamics.

Chapter Goal: To establish a connection between force and motion.



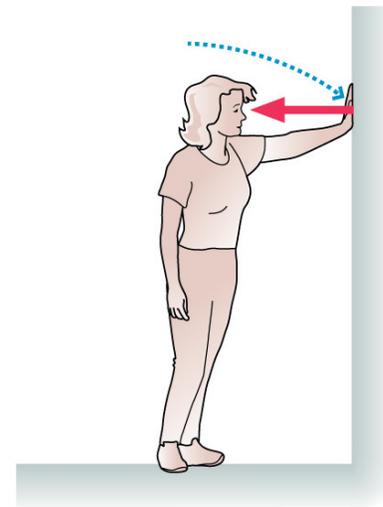
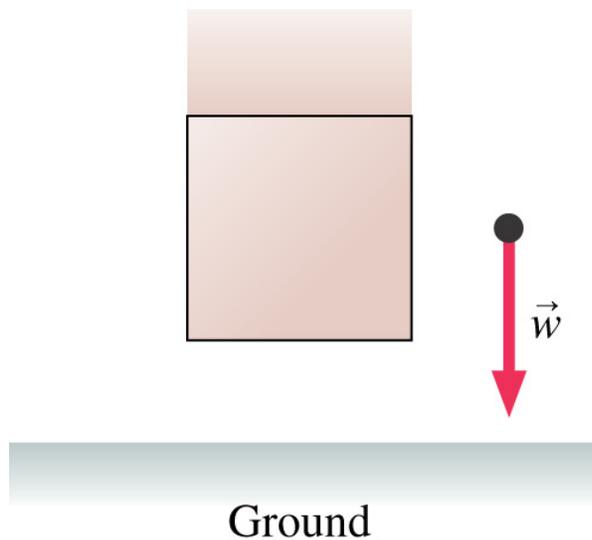
Chapter 5. Force and Motion

Topics:

- Force
- A Short Catalog of Forces
- Identifying Forces
- What Do Forces Do?
- Newton's Second Law
- Newton's First Law
- Free-Body Diagrams

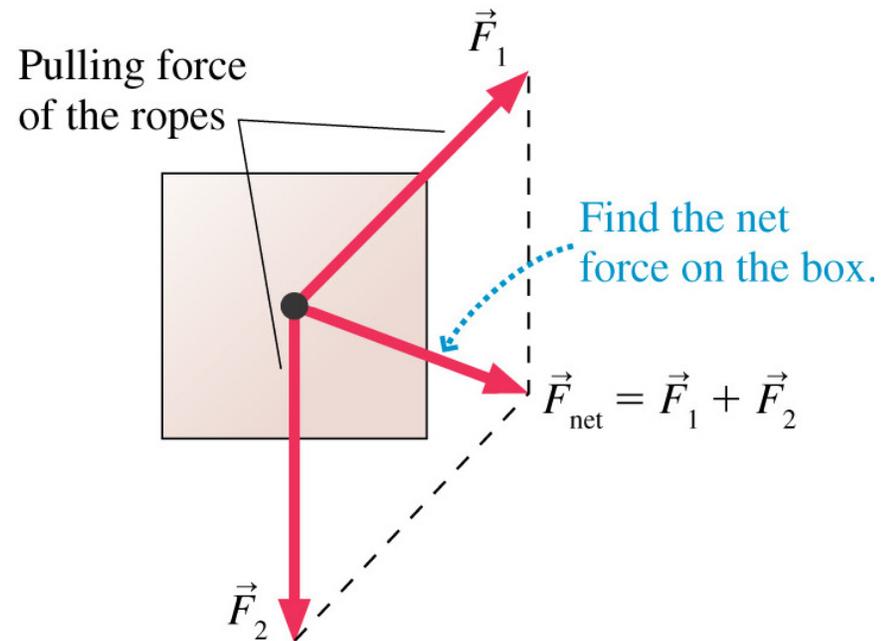
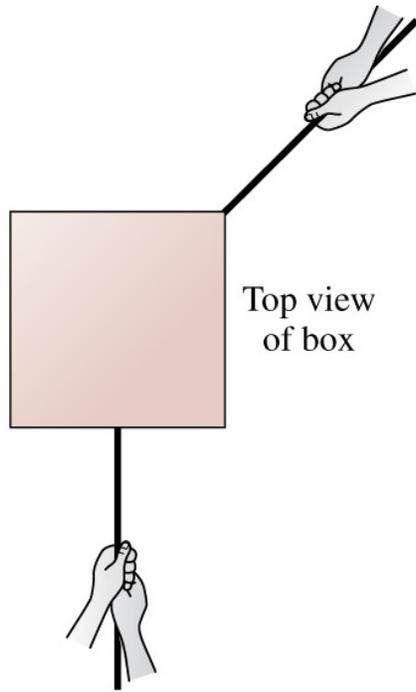
Force: Properties

1. Push or Pull
2. Acts on an object
3. Force is a **vector**
4. Force is either a contact force or long range force



Force: Properties

Force is a vector – The net force is the vector sum of the individual forces



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How can we find the individual force?

Major Forces:

1. Weight – gravitational force

pulls the objects down – determines its direction

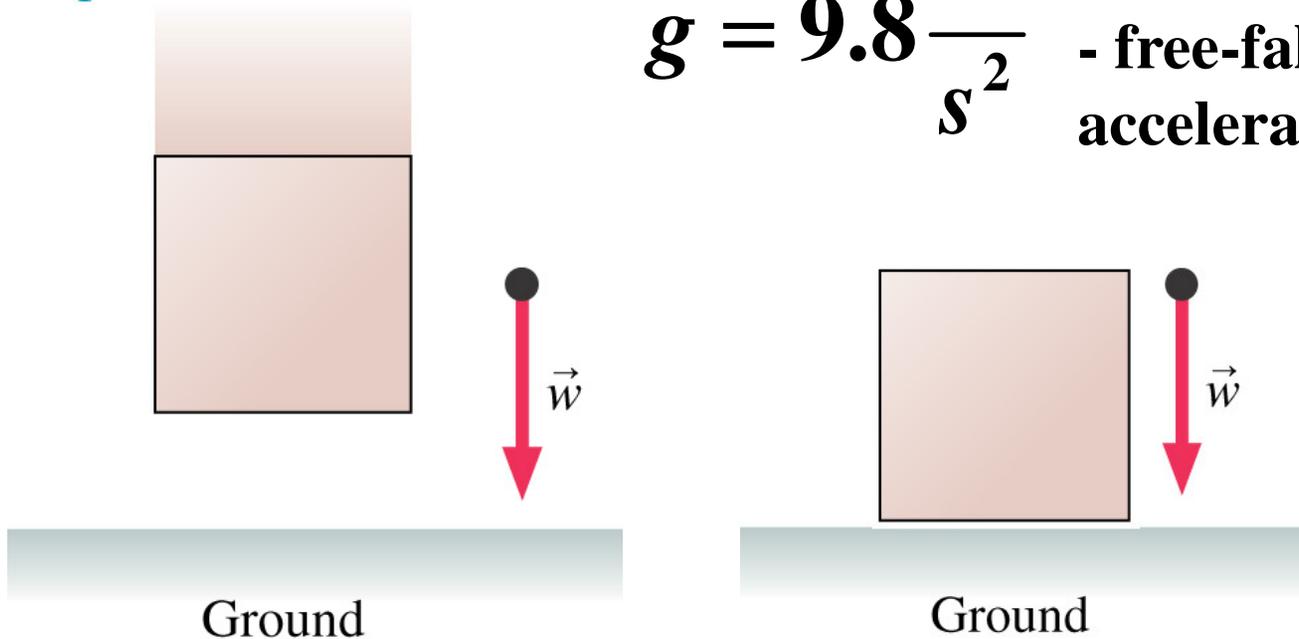
magnitude:

$$\vec{w} = m\vec{g}$$

m - Mass of the object

$g = 9.8 \frac{m}{s^2}$ - free-fall acceleration

The weight force pulls the box down.



Major Forces:

1. Weight – gravitational force

$$\vec{w} = m\vec{g}$$

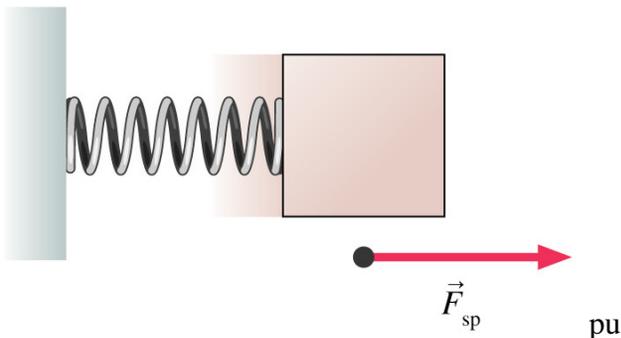
2. Spring Force

$$F_{sp} = kx$$

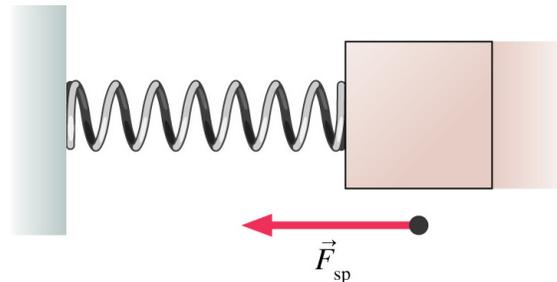
k - coefficient, which depends only on geometric parameters of the spring

$x = |\Delta l|$ - change in the length of the spring

A compressed spring exerts a pushing force on an object.



A stretched spring exerts a pulling force on an object.



Major Forces:

1. Weight – gravitational force

$$\vec{w} = m\vec{g}$$

2. Spring Force

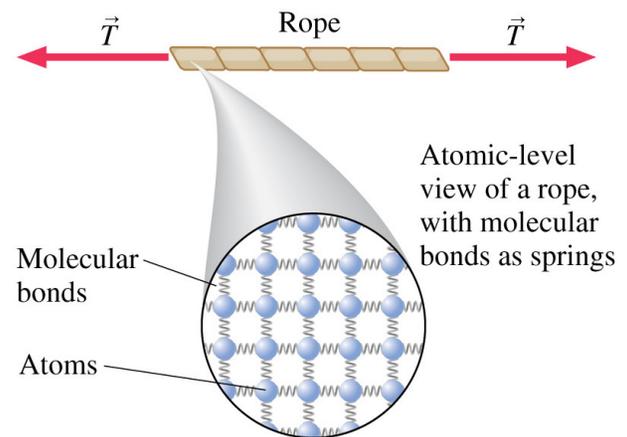
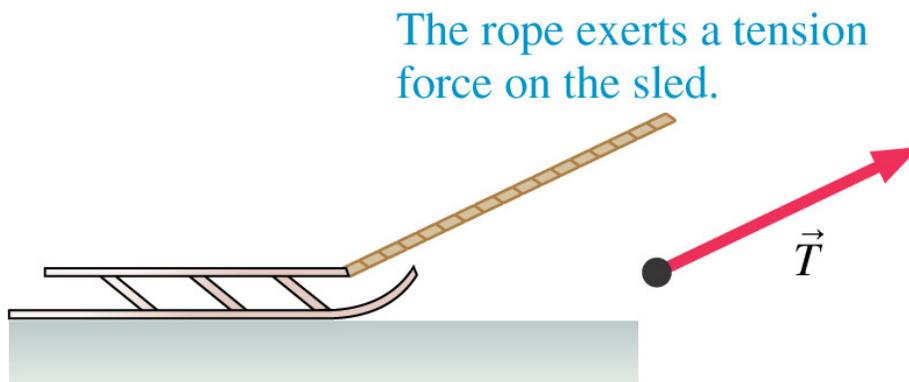
$$F_{sp} = kx$$

3. Tension Force

$$\vec{T}$$

direction is always in the direction of the rope

magnitude - usually found from the condition of equilibrium



Major Forces:

1. Weight – gravitational force

$$\vec{w} = m\vec{g}$$

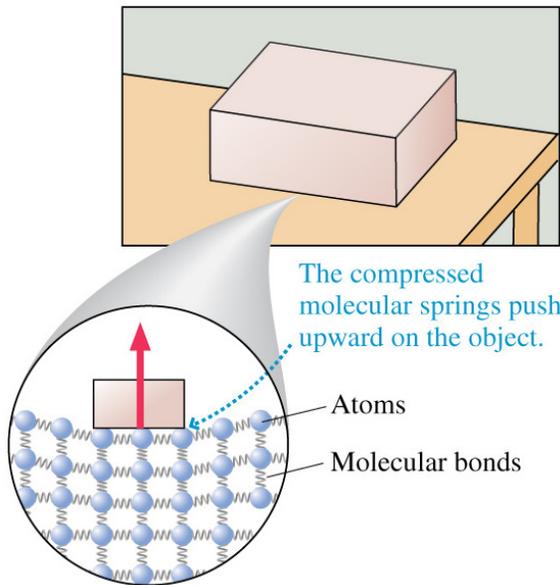
2. Spring Force $F_{sp} = kx$

3. Tension Force \vec{T}

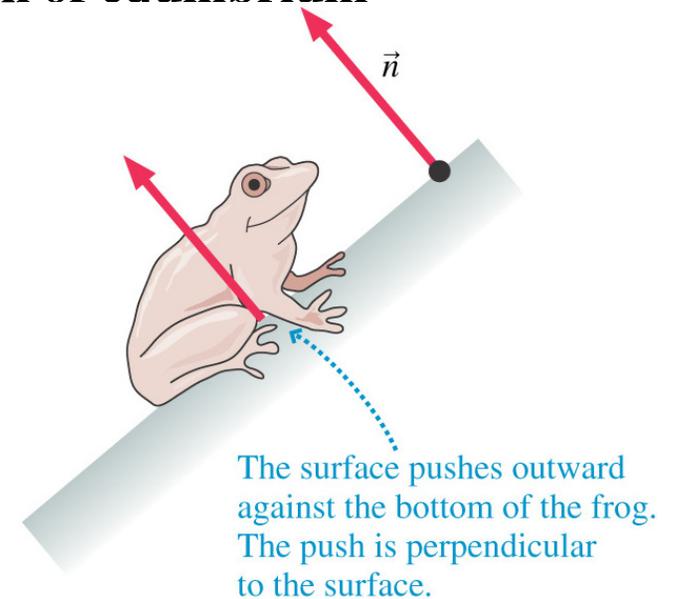
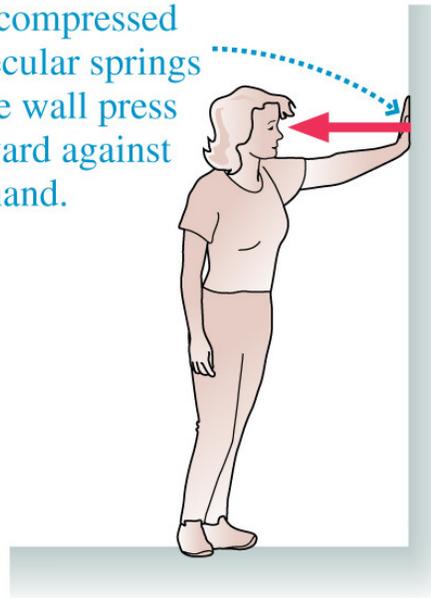
4. Normal Force \vec{n}

direction is always perpendicular to the surface

magnitude - usually found from the condition of equilibrium



The compressed molecular springs in the wall press outward against her hand.



Major Forces:

1. Weight – gravitational force

$$\vec{w} = m\vec{g}$$

2. Spring Force

$$F_{sp} = kx$$

3. Tension Force

$$\vec{n}$$

$$\vec{T}$$

4. Normal Force

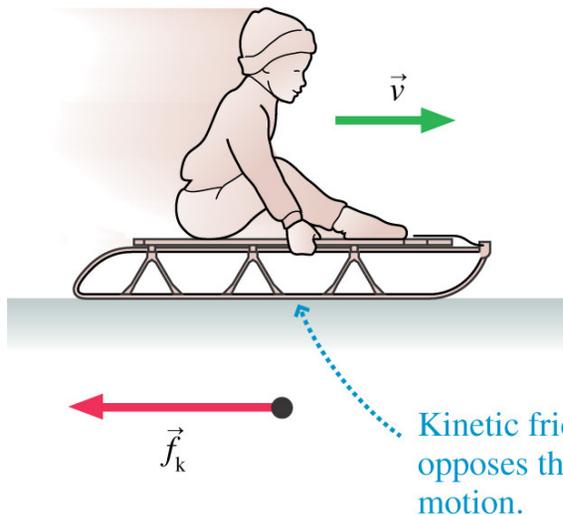
5. Friction

$$\vec{f}_k$$

- Kinetic friction – opposes the motion

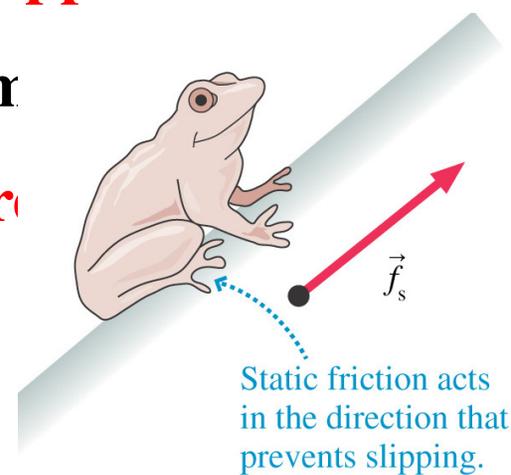
$$\vec{f}_s$$

direction – opposite the velocity vector



prevent the m

opposite the dir



the object would

Major Forces:

1. Weight – gravitational force

$$\vec{w} = m\vec{g}$$

2. Spring Force $F_{sp} = kx$

3. Tension Force \vec{T}

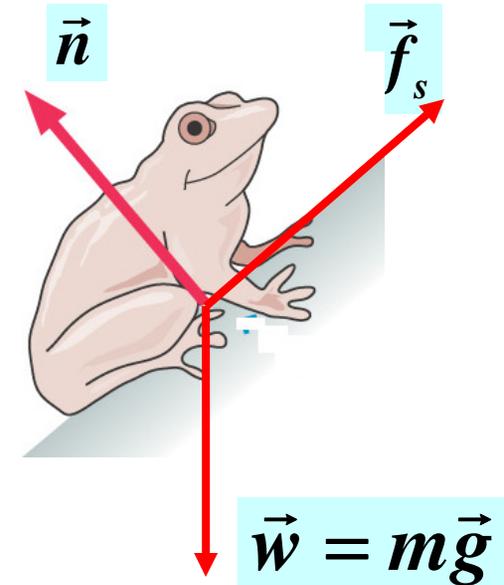
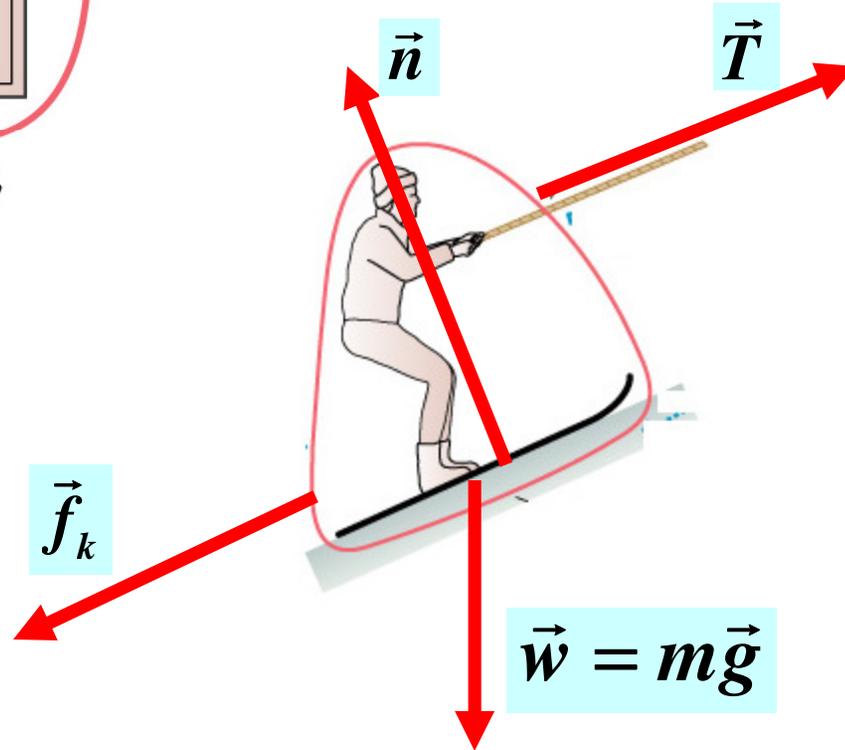
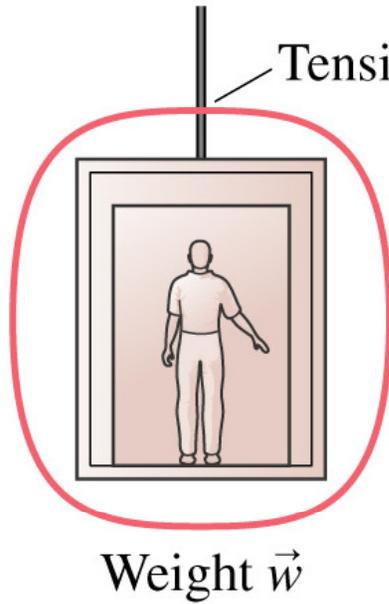
4. Normal Force \vec{n}

5. Friction

- kinetic friction \vec{f}_k

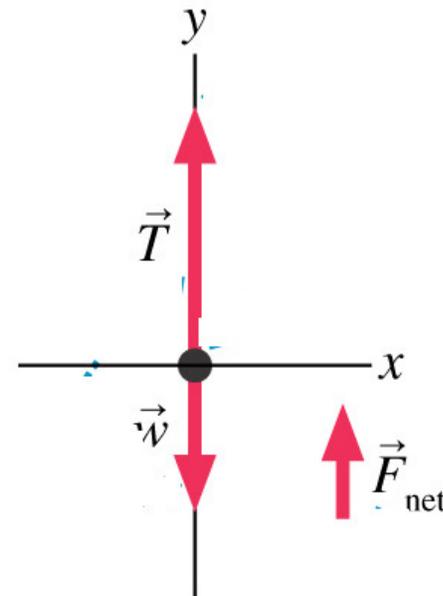
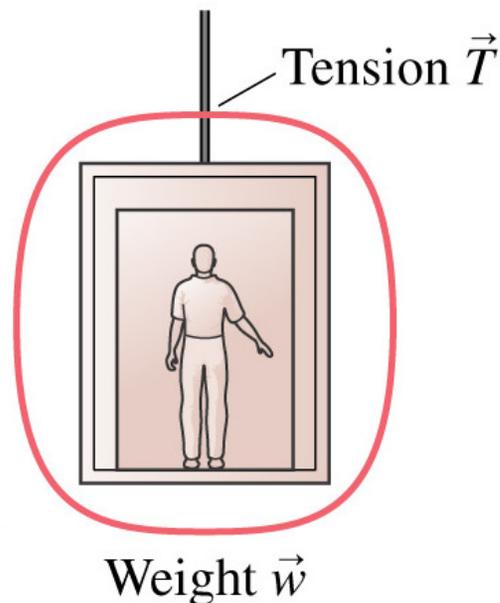
- static friction \vec{f}_s

Force Identification



Free-Body Diagram

- 1) Object – as a particle
- 2) Identify all the forces
- 3) Find the net force (vector sum of all individual forces)
- 4) Find the acceleration of the object (second Newton's law)
- 5) With the known acceleration find kinematics of the object

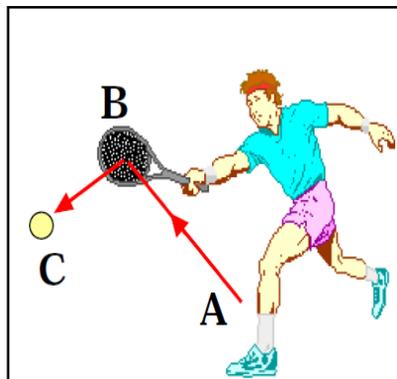


Newton's Laws of Motion

It was Isaac Newton (1642-1727) who realized the importance of force and its connection with motion.

Three Laws of motion

- 1st Law: inertia
- 2nd Law: change in motion
- 3rd Law: action and reaction pairs

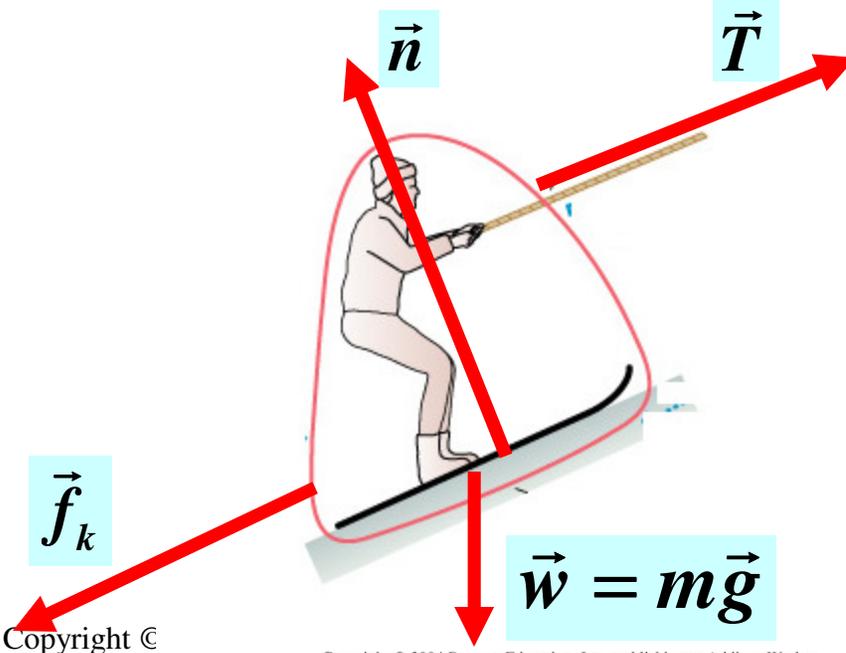


Newton's Second Law

An object of mass m subject to forces undergo an acceleration given by

$$\vec{F}_1, \vec{F}_2, \dots$$

$$\vec{a} = \frac{\vec{F}_{net}}{m}$$

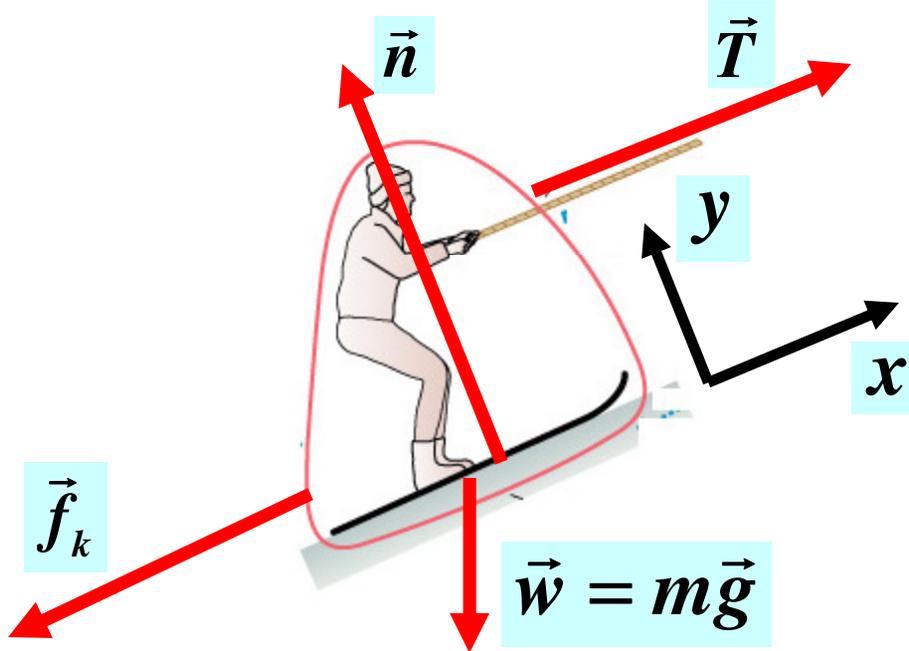


$$\vec{a} = \frac{\vec{w} + \vec{n} + \vec{T} + \vec{f}_k}{m}$$

Newton's Second Law

$$\vec{a} = \frac{\vec{F}_{net}}{m}$$

$$\vec{a} = \frac{\vec{w} + \vec{n} + \vec{T} + \vec{f}_k}{m}$$



It is convenient to introduce coordinate system and write the Newton's second law in terms of vector components

No motion in y-direction:

$$a_y = 0$$

$$w_y + n = 0$$

For motion in x-direction:

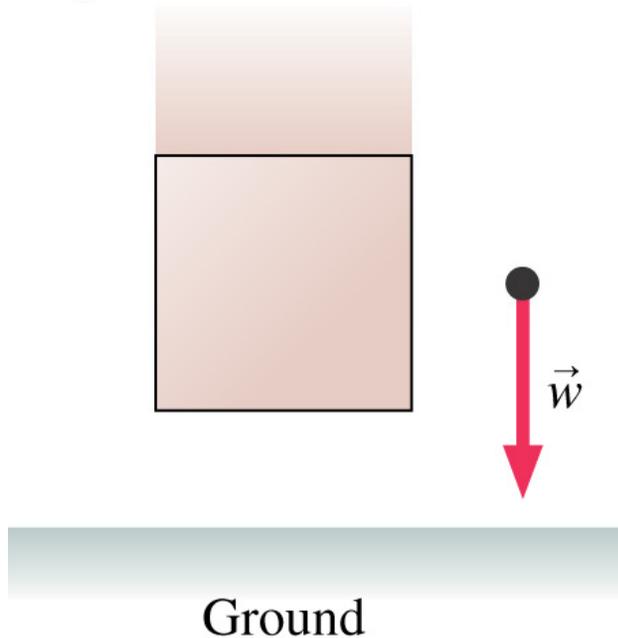
$$ma_x = w_x + T - f_k$$

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Free-fall motion

The weight force pulls the box down.



$$\vec{w} = m\vec{g}$$

Then from the second

New

$$\vec{a} = \frac{\vec{w}}{m} = \frac{m\vec{g}}{m} = \vec{g}$$

$$g = 9.8 \frac{m}{s^2}$$

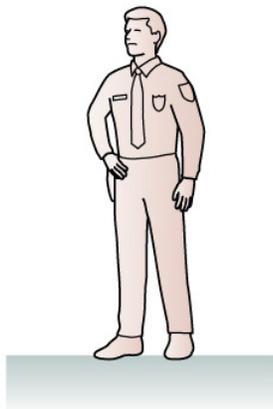
The acceleration is the same for all objects (does not depend on the mass of the object)

Newton's First Law

An object that is at rest will remain at rest, or an object that is moving will continue to move in a straight line with constant velocity, if and only if the net force acting on the object is zero.

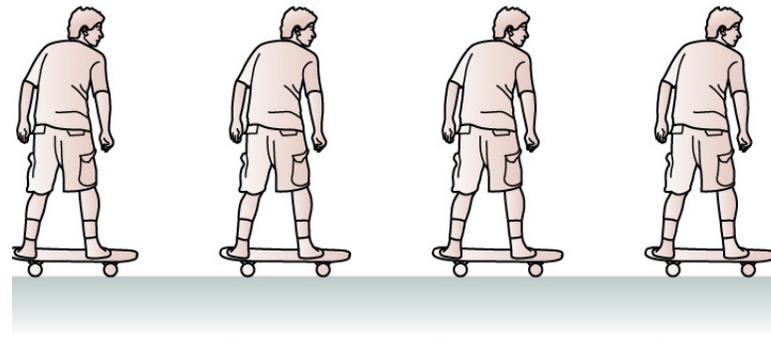
$\vec{F}_{net} = 0$ then $\vec{a} = 0$ velocity is constant

Static equilibrium



Cop. $\vec{v} = \vec{0}$ ●
 $\vec{a} = \vec{0}$

Dynamic equilibrium



\vec{v} ● → ● → ● → ●
 $\vec{a} = \vec{0}$

Inertial reference frames

Inertial reference frame is the coordinate system in which Newton's laws are valid.

The earth is an inertial reference frame

Any other coordinate systems, which are traveling with constant velocity with respect to the earth is an inertial reference frame

Car traveling with constant velocity is an inertial reference frame

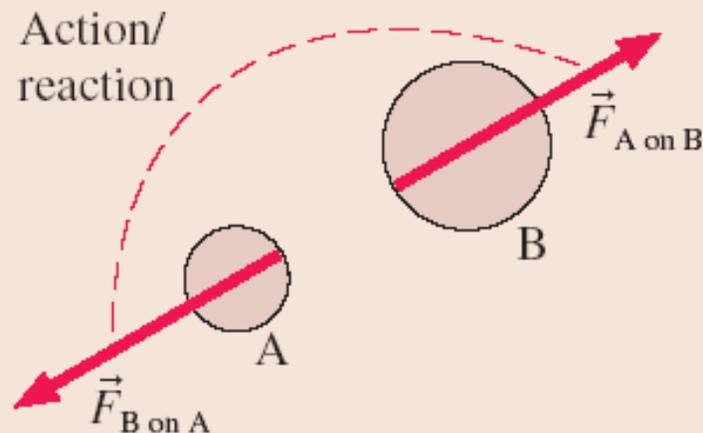
Car traveling with acceleration is **NOT an inertial reference frame (violation of Newton's law)**

Newton's Third Law

Every force occurs as one member of an **action/reaction pair** of forces. The two members of an action/reaction pair:

- Act on two *different* objects.
- Are equal in magnitude but opposite in direction:

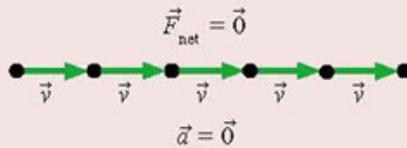
$$\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$$



Chapter 5. Summary

Newton's First Law

An object at rest will remain at rest, or an object that is moving will continue to move in a straight line with constant velocity, if and only if the net force on the object is zero.



The first law tells us that no “cause” is needed for motion. Uniform motion is the “natural state” of an object.

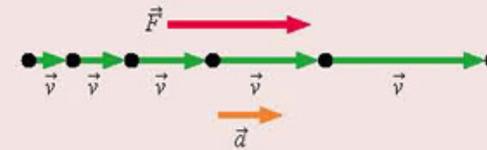
Newton's laws are valid only in inertial reference frames.

Newton's Second Law

An object with mass m will undergo acceleration

$$\vec{a} = \frac{1}{m} \vec{F}_{\text{net}}$$

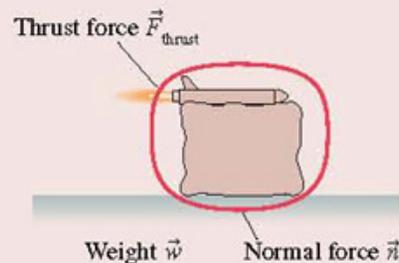
where $\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$ is the vector sum of all the individual forces acting on the object.



The second law tells us that a net force causes an object to accelerate. This is the connection between force and motion that we are seeking.

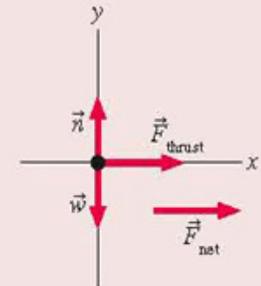
Identifying Forces

Forces are identified by locating the points where the environment touches the system. These are points where contact forces are exerted. In addition, objects with mass feel a long-range weight force.



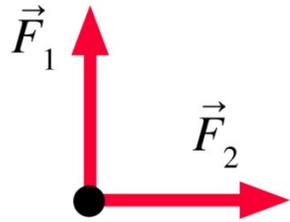
Free-Body Diagrams

A free-body diagram represents the object as a particle at the origin of a coordinate system. Force vectors are drawn with their tails on the particle. The net force vector is drawn beside the diagram.

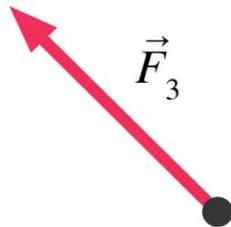


Chapter 5. Questions

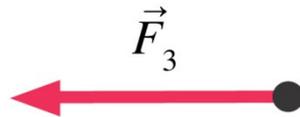
Two of three forces exerted on an object are shown. The net force points to the left. What is the missing third force?



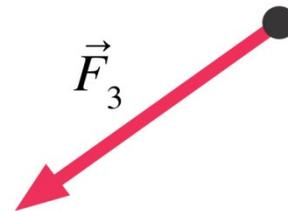
Two forces exerted on an object



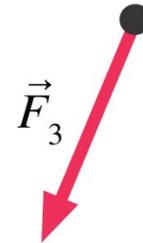
(a)



(b)

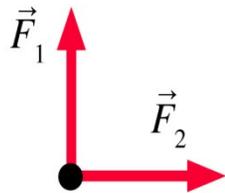


(c)

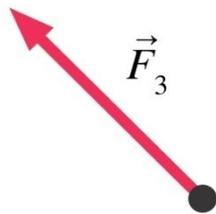
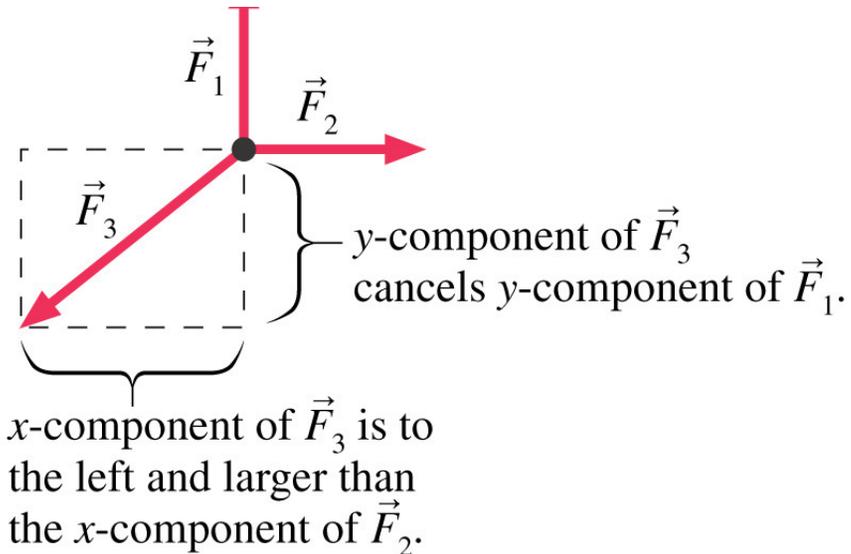


(d)

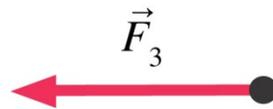
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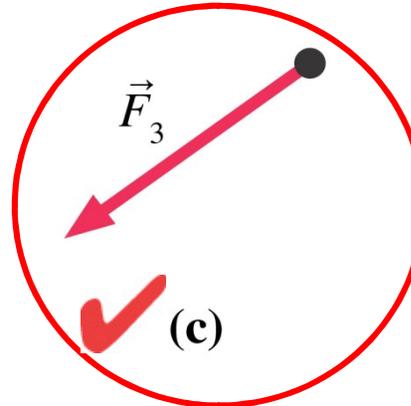
Two forces exerted on an object



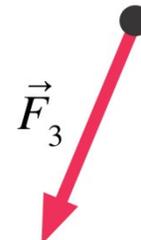
(a)



(b)



(c)



(d)

You've just kicked a rock, and it is now sliding across the ground about 2 meters in front of you. Which of these forces act on the ball?

- A. Gravity, acting downward
- B. The normal force, acting upward
- C. The force of the kick, acting in the direction of motion
- D. Friction, acting opposite the direction of motion
- E. A, B, and D but not C.

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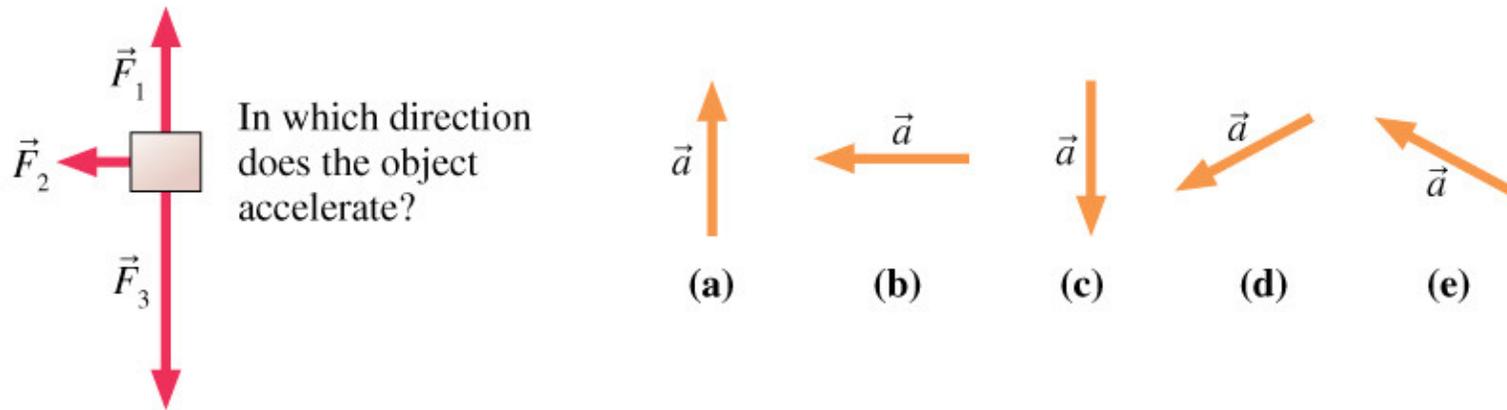
Two rubber bands stretched the standard distance cause an object to accelerate at 2 m/s^2 . Suppose another object with twice the mass is pulled by four rubber bands stretched the standard length. The acceleration of this second object is

- A. 16 m/s^2 .
- B. 8 m/s^2 .
- C. 4 m/s^2 .
- D. 2 m/s^2 .
- E. 1 m/s^2 .

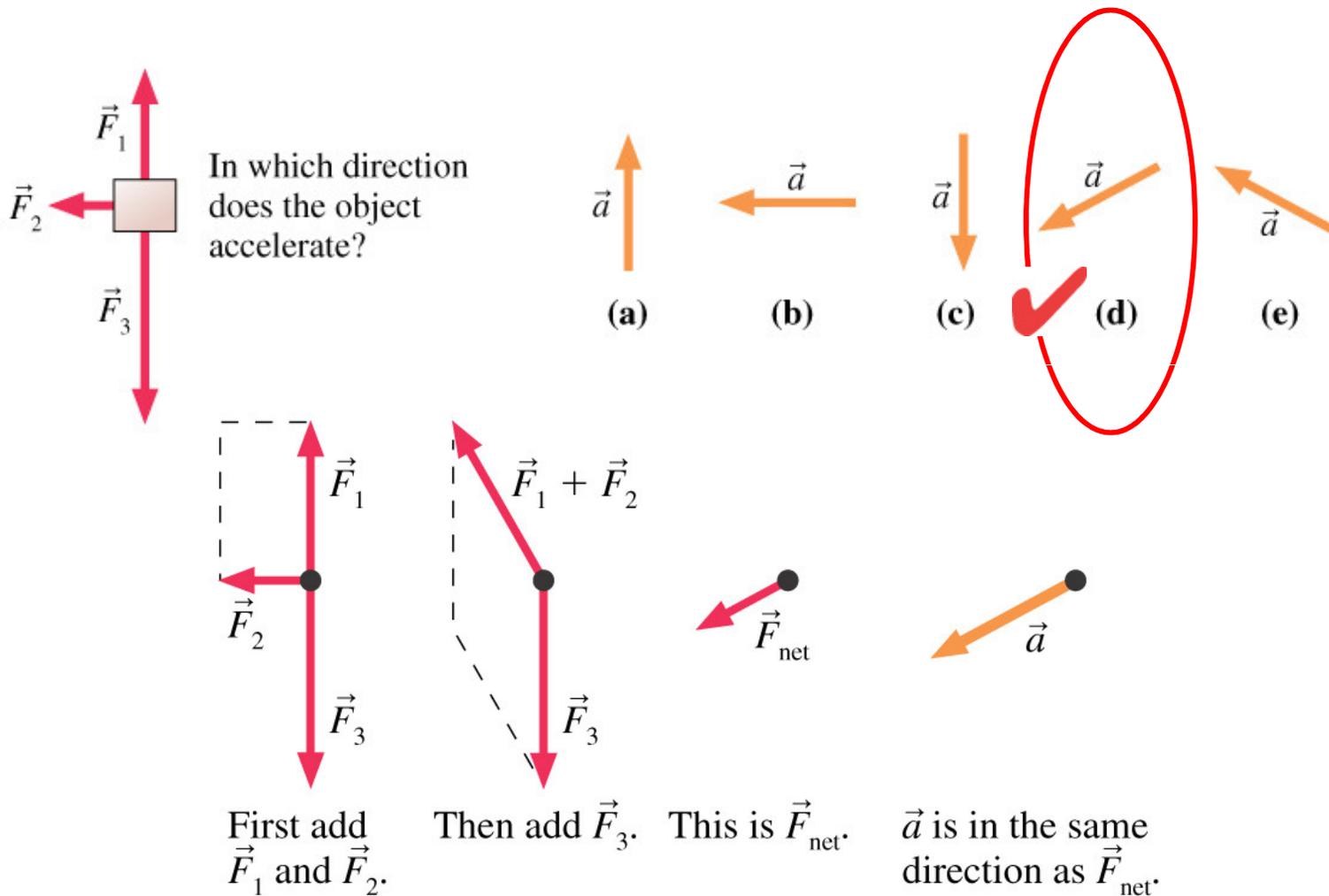
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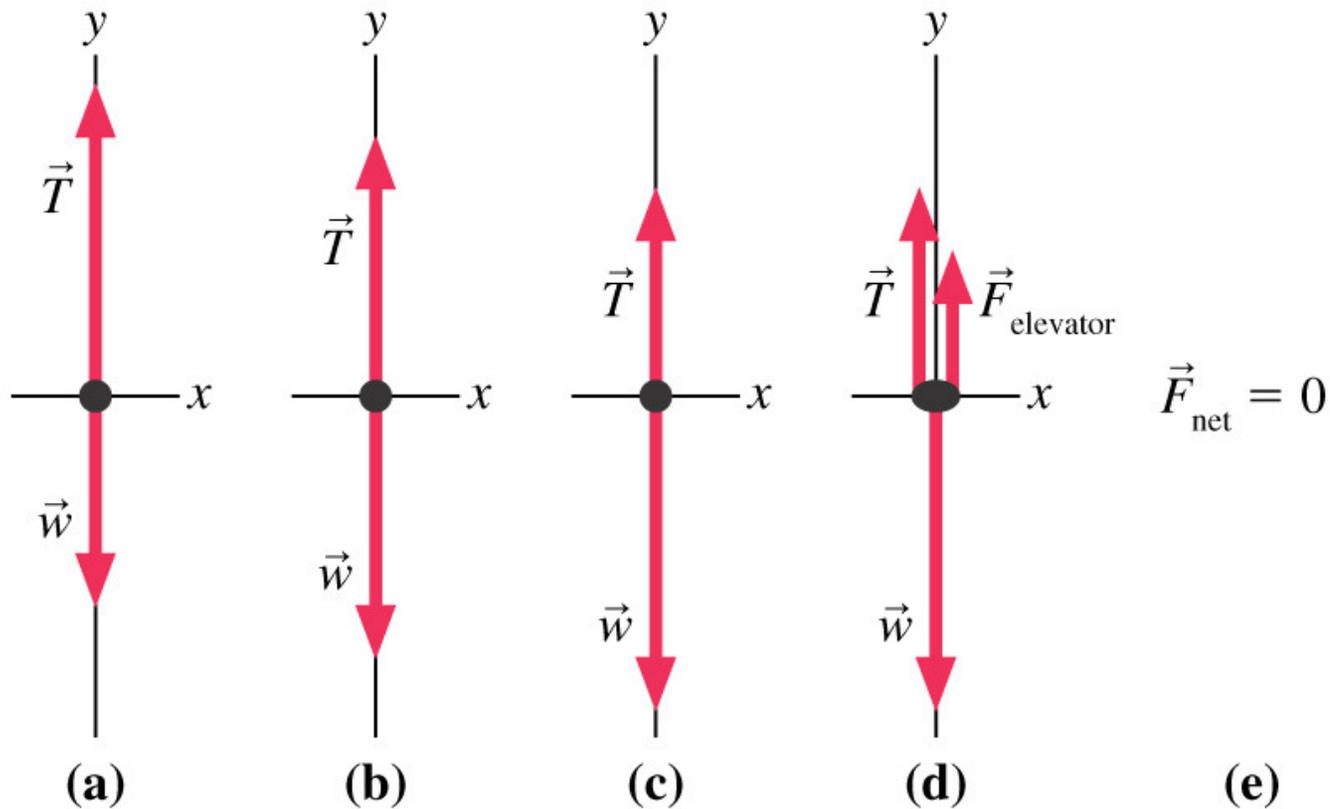
Three forces act on an object. In which direction does the object accelerate?



Three forces act on an object. In which direction does the object accelerate?



An elevator suspended by a cable is moving upward and slowing to a stop. Which free-body diagram is correct?



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