Chapter 26

# The Refraction of Light: Lenses and Optical Instruments

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Light travels through a vacuum at a speed  $c = 3.00 \times 10^8 \text{ m/s}$ 

Light travels through materials at a speed less than its speed in a vacuum.

### DEFINITION OF THE INDEX OF REFRACTION

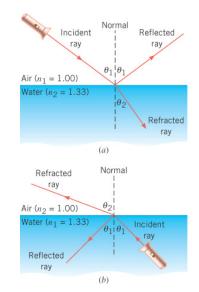
The index of refraction of a material is the ratio of the speed of light in a vacuum to the speed of light in the material:

 $n = \frac{\text{Speed of light in vacuum}}{\text{Speed of light in the material}} = \frac{c}{v}$ 

#### 26.1 The Index of Refraction

Substance	Index of Refraction, <i>r</i>
Solids at 20 °C	
Diamond	2.419
Glass, crown	1.523
Ice (0 °C)	1.309
Sodium chloride	1.544
Quartz	
Crystalline	1.544
Fused	1.458
Liquids at 20 °C	
Benzene	1.501
Carbon disulfide	1.632
Carbon tetrachloride	1.461
Ethyl alcohol	1.362
Water	1.333
Gases at 0 °C, 1 atm	
Air	1.000 293
Carbon dioxide	1.000 45
Oxygen, O <sub>2</sub>	1.000 271
Hydrogen, H <sub>2</sub>	1.000 139

#### 26.2 Snell's Law and the Refraction of Light



### SNELL'S LAW

### SNELL'S LAW OF REFRACTION

When light travels from a material with one index of refraction to a material with a different index of refraction, the angle of incidence is related to the angle of refraction by

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

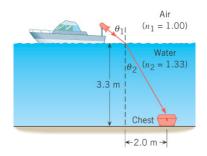
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#### 26.2 Snell's Law and the Refraction of Light

#### **Example 1** Determining the Angle of Refraction (a) $\sin \theta_2 = \frac{n_1 \sin \theta_1}{n_2} = \frac{(1.00) \sin 46^\circ}{1.33} = 0.54$ A light ray strikes an air/water surface at an Norma Incident Reflected Reflected Incident angle of 46 degrees with respect to the rav ray rav normal. Find the angle of refraction when $\theta_2 = 33^\circ$ Air $(n_1 = 1.00)$ Air $(n_1 = 1.00)$ the direction of the ray is (a) from air to ter $(n_2 = 1.33)$ Vater $(n_2 = 1.33)$ water and (b) from water to air. Refracte Refracte (a)(*a*) $\sin \theta_2 = \frac{n_1 \sin \theta_1}{n_2} = \frac{(1.33) \sin 46^\circ}{1.00} = 0.96$ Normal Norma Refracted Refracted (b) ray ray Air $(n_2 = 1.00)$ Air $(n_2 = 1.00)$ Reflected Reflected rav ray $\theta_2 = 74^\circ$ (b) (b) 5

#### 26.2 Snell's Law and the Refraction of Light

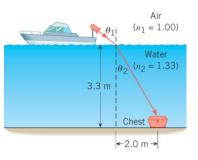
### APPARENT DEPTH



### *Example 2* Finding a Sunken Chest

The searchlight on a yacht is being used to illuminate a sunken chest. At what angle of incidence should the light be aimed?

#### 26.2 Snell's Law and the Refraction of Light



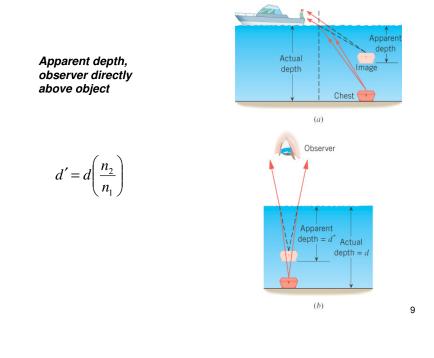
 $\theta_2 = \tan^{-1}(2.0/3.3) = 31^\circ$ 

$$\sin \theta_1 = \frac{n_2 \sin \theta_2}{n_1} = \frac{(1.33) \sin 31^\circ}{1.00} = 0.69$$

$$\theta_1 = 44^\circ$$

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#### 26.2 Snell's Law and the Refraction of Light



### 26.2 Snell's Law and the Refraction of Light

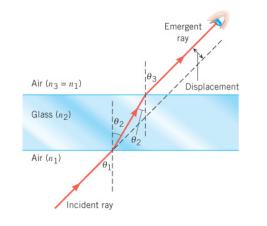
### Conceptual Example 4 On the Inside Looking Out

A swimmer is under water and looking up at the surface. Someone holds a coin in the air, directly above the swimmer's eyes. To the swimmer, the coin appears to be at a certain height above the water. Is the apparent height of the coin greater, less than, or the same as its actual height?

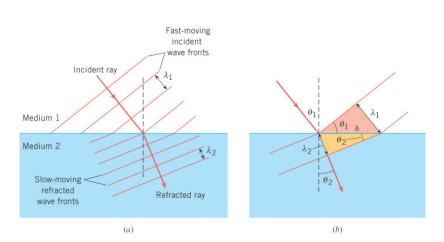
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#### 26.2 Snell's Law and the Refraction of Light



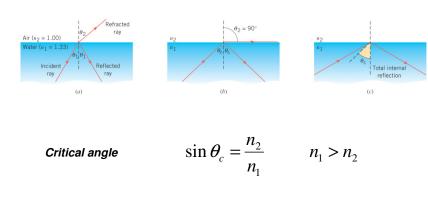


### 26.2 Snell's Law and the Refraction of Light



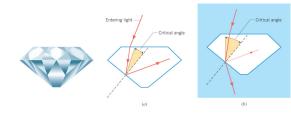
THE DERIVATIN OF SNELL'S LAW

When light passes from a medium of larger refractive index into one of smaller refractive index, the refracted ray bends away from the normal.



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#### 26.3 Total Internal Reflection



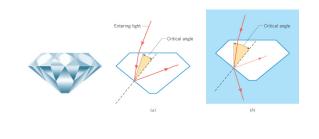
(a) 
$$\theta_c = \sin^{-1} \left( \frac{n_2}{n_1} \right) = \sin^{-1} \left( \frac{1.00}{2.42} \right) = 24.4^\circ$$

(b) 
$$\theta_c = \sin^{-1} \left( \frac{n_2}{n_1} \right) = \sin^{-1} \left( \frac{1.33}{2.42} \right) = 33.3^\circ$$

#### 26.3 Total Internal Reflection

#### **Example 5** Total Internal Reflection

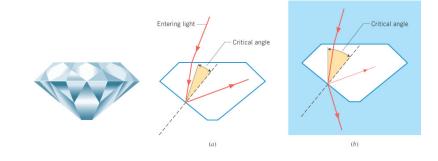
A beam of light is propagating through diamond and strikes the diamond-air interface at an angle of incidence of 28 degrees. (a) Will part of the beam enter the air or will there be total internal reflection? (b) Repeat part (a) assuming that the diamond is surrounded by water.



#### 26.3 Total Internal Reflection

### Conceptual Example 6 The Sparkle of a Diamond

The diamond is famous for its sparkle because the light coming from it glitters as the diamond is moved about. Why does a diamond exhibit such brilliance? Why does it lose much of its brilliance when placed under water?

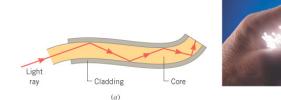


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 $\theta_1 = 45^\circ$ 

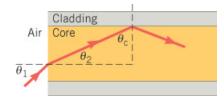
(*a*)

### 26.3 Total Internal Reflection





(*b*)



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Unpolarized incident light Polarized reflected light  $\theta_B$   $\theta_B$   $\theta_B$   $n_1$   $\theta_2$  90°  $n_2$ Partially polarized refracted light

45

45

45

(*b*)

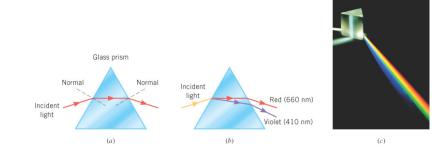
Brewster's law



### 26.5 The Dispersion of Light: Prisms and Rainbows

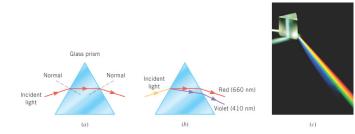
The net effect of a prism is to change the direction of a light ray.

Light rays corresponding to different colors bend by different amounts.



Light ray

#### 26.5 The Dispersion of Light: Prisms and Rainbows

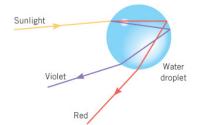


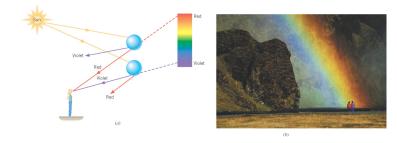
#### Table 26.2 Indices of Refraction n of Crown Glass at Various Wavelengths

Approximate Color	Wavelength in Vacuum (nm)	Index of Refraction, n
Red	660	1.520
Orange	610	1.522
Yellow	580	1.523
Green	550	1.526
Blue	470	1.531
Violet	410	1.538

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#### 26.5 The Dispersion of Light: Prisms and Rainbows

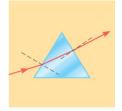




#### 26.5 The Dispersion of Light: Prisms and Rainbows

*Conceptual Example 7* The Refraction of Light Depends on Two Refractive Indices

It is possible for a prism to bend light upward, downward, or not at all. How can the situations depicted in the figure arise?





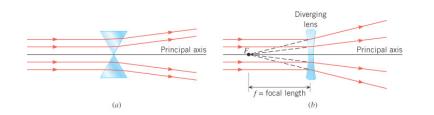
#### 26.6 Lenses

Lenses refract light in such a way that an image of the light source is formed.

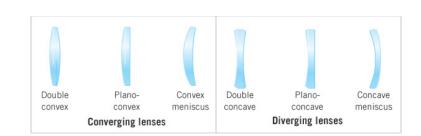
With a converging lens, paraxial rays that are parallel to the principal axis converge to the focal point.



With a diverging lens, paraxial rays that are parallel to the principal axis appear to originate from the focal point.



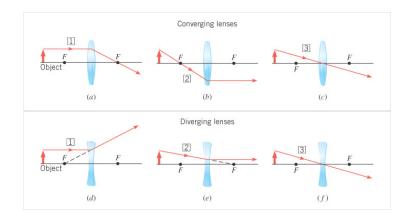




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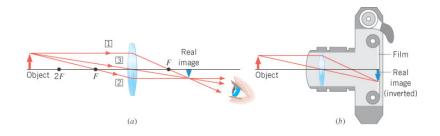
### 26.7 The Formation of Images by Lenses

**RAY DIAGRAMS** 



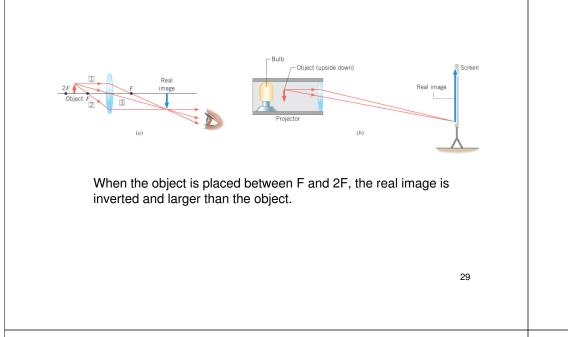
### 26.7 The Formation of Images by Lenses

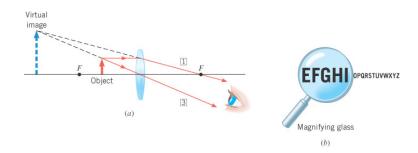
### IMAGE FORMATION BY A CONVERGING LENS



In this example, when the object is placed further than twice the focal length from the lens, the real image is inverted and smaller than the object.

#### 26.7 The Formation of Images by Lenses



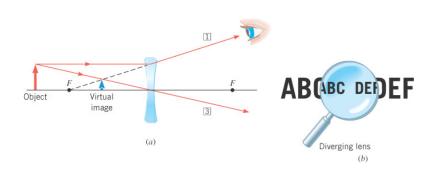


When the object is placed between F and the lens, the virtual image is upright and larger than the object.

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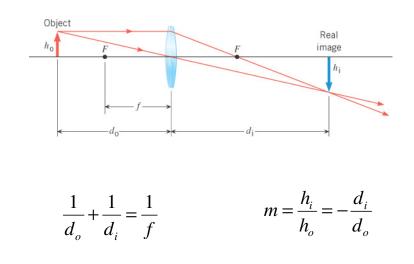






A diverging lens always forms an upright, virtual, diminished image.

#### 26.8 The Thin-Lens Equation and the Magnification Equation



### Summary of Sign Conventions for Lenses

- f is + for a converging lens.
- f is for a diverging lens.
- $d_{a}$  is + if the object is to the left of the lens.
- $d_{a}$  is if the object is to the right of the lens.

 $d_i$  is + for an image formed to the right of the lens (real image).

 $d_i$  is – for an image formed to the left of the lens (virtual image).

m is + for an upright image.

m is – for an inverted image.



### Example 9 The Real Image Formed by a Camera Lens

A 1.70-m tall person is standing 2.50 m in front of a camera. The camera uses a converging lens whose focal length is 0.0500 m. (a) Find the image distance and determine whether the image is real or virtual. (b) Find the magnification and height of the image on the film.

$$\frac{1}{d} = \frac{1}{f} - \frac{1}{d} = \frac{1}{0.0500 \,\mathrm{m}} - \frac{1}{2.50 \,\mathrm{m}} = 19.6 \,\mathrm{m}^{-1}$$

 $d_i = 0.0510 \,\mathrm{m}$ real image

(b) 
$$m = -\frac{d_i}{d_o} = -\frac{0.0510 \text{ m}}{2.50 \text{ m}} = -0.0204$$

$$h_i = mh_o = (-0.0204)(2.50 \text{ m}) = -0.0347 \text{ m}$$

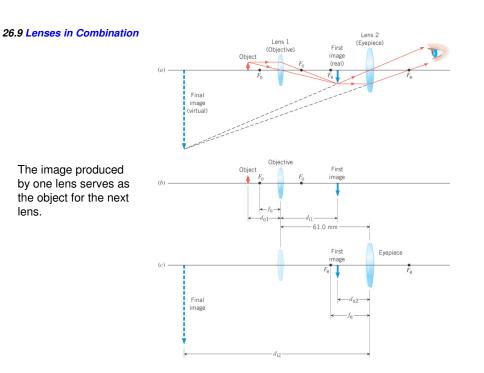


26.10 The Human Eve

(a)

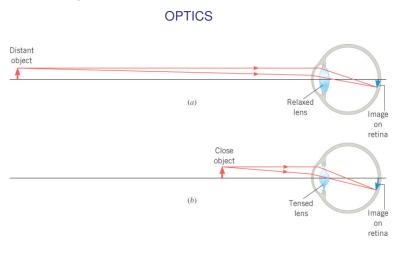
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Vitreous humor Aqueous humor Retina-Lens Suspensory ligament Cornea Ciliary Optic muscle nerve Iris







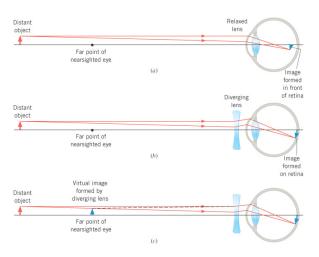


The lens only contributes about 20-25% of the refraction, but its function is important.

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#### 26.10 The Human Eye

### NEARSIGNTEDNESS

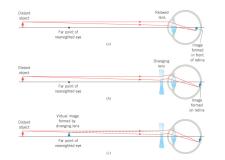


The lens creates an image of the distance object at the far point of the nearsighted eye.

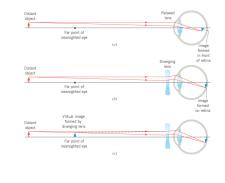
### 26.10 The Human Eye

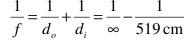
### Example 12 Eyeglasses for the Nearsighted Person

A nearsighted person has a far point located only 521 cm from the eye. Assuming that eyeglasses are to be worn 2 cm in front of the eye, find the focal length needed for the diverging lens of the glasses so the person can see distant objects.



### 26.10 The Human Eye

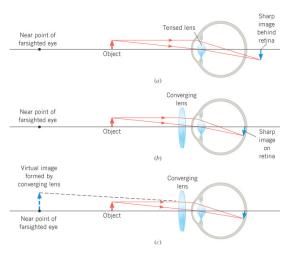




 $f = -519 \,\mathrm{cm}$ 

40

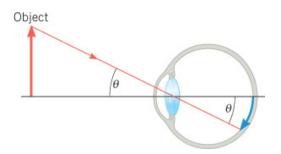
### FARSIGNTEDNESS



The lens creates an image of the close object at the near point of the farsighted eye.

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#### 26.11 Angular Magnification and the Magnifying Glass



The size of the image on the retina determines how large an object appears to be.

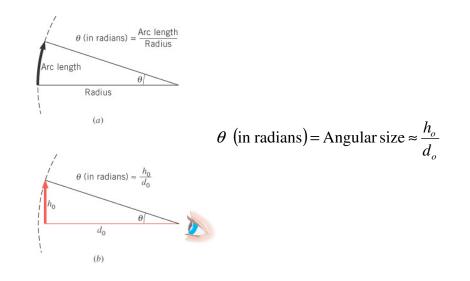
### 26.10 The Human Eye

### THE REFRACTIVE POWER OF A LENS – THE DIOPTER

Optometrists who prescribe correctional lenses and the opticians who make the lenses do not specify the focal length. Instead they use the concept of *refractive power*.

Refractive power (in diopters) =  $\frac{1}{f$  (in meters)





### 26.11 Angular Magnification and the Magnifying Glass

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### *Example 14* A Penny and the Moon

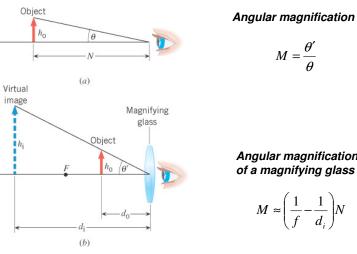
Compare the angular size of a penny held at arms length with that of the moon.

Penny

$$\theta \approx \frac{h_o}{d_o} = \frac{1.9 \text{ cm}}{71 \text{ cm}} = 0.027 \text{ rad}$$

Moon

$$\theta \approx \frac{h_o}{d_o} = \frac{3.5 \times 10^6 \text{ m}}{3.9 \times 10^8 \text{ m}} = 0.0090 \text{ rad}$$



Angular magnification of a magnifying glass

$$M \approx \left(\frac{1}{f} - \frac{1}{d_i}\right) N$$

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#### 26.12 The Compound Microscope

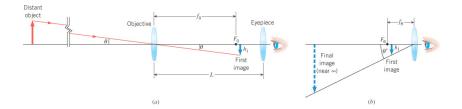


To increase the angular magnification beyond that possible with a magnifying glass, an additional converging lens can be included to "premagnify" the object.

> Angular magnification of a compound microscope

 $M \approx -\frac{(L-f_e)N}{f_a f_e}$ 

#### 26.13 The Telescope



Angular magnification of an astronomical telescope  $M \approx -\frac{f_o}{f_e}$ 

#### 26.14 Lens Aberrations

#### 26.14 Lens Aberrations

